

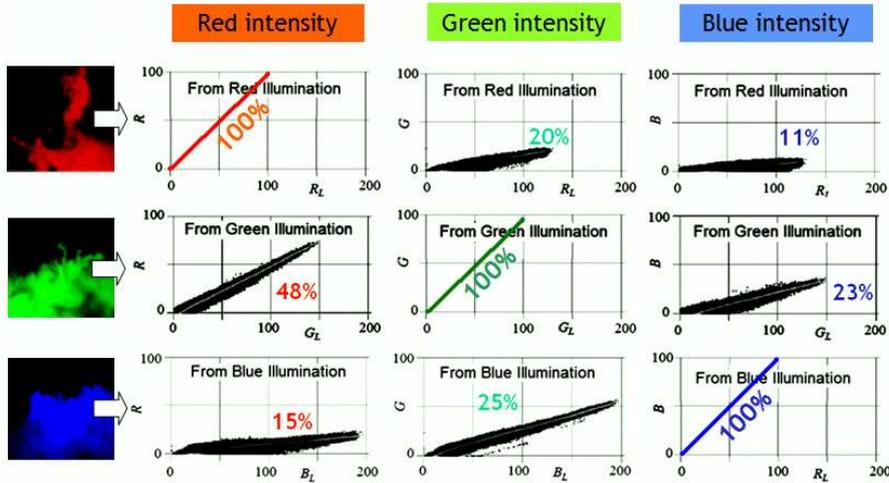
# Color contamination matrix property assessment for improvement of colored smoke PIV

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A single-camera color PIV system that can acquire PIV data of three separated layers has been re-designed, purposing improvement of wind tunnel applicability. We target smoke image that has particle-per-pixel values higher than unity. The system constitutes of a high-power color-coding illuminator and a digital color high-speed video camera. RGB values in recorded image involves severe color contaminations due to five optical and digital sequences (**Fig. 1**). To quantify this, a snapshot calibration is proposed to describe the contamination matrix equation (**Eq. (1)**). Taking the inverse matrix (**Eq. (2)**) allows in-plane PIV in each color layer to be accurately implemented. We also derive mathematical limits to operate the colored smoke PIV, which is explained by the matrix property (**Eq (3)**). Feasibility of the proposed method has been demonstrated by application to a turbulent wake behind a Delta wing (**Fig. 2**) and also to a boundary layer flow along heated chocolate.



**Fig. 1** Color contamination property for a water mist in air projected by a sheet of color light

*Color contamination matrix equation:*

$$\begin{bmatrix} R \\ G \\ B \end{bmatrix} = \begin{bmatrix} 1 & a_3 & a_5 \\ a_1 & 1 & a_6 \\ a_2 & a_4 & 1 \end{bmatrix} \begin{bmatrix} R_L \\ G_L \\ B_L \end{bmatrix} + \begin{bmatrix} b_1 \\ b_2 \\ b_3 \end{bmatrix}, \quad (1)$$

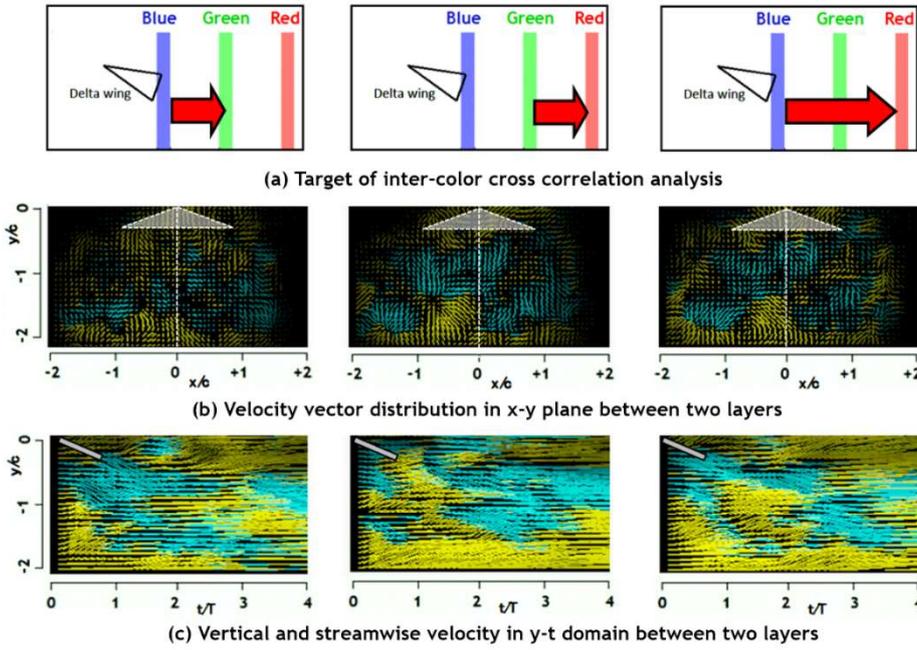
1 *Inverse matrix equation for estimating smoke density in three colored layers*

$$2 \begin{bmatrix} R_L \\ G_L \\ B_L \end{bmatrix} = \frac{1}{K} \begin{bmatrix} 1-a_3a_6 & a_3a_5-a_4 & a_4a_6-a_5 \\ a_2a_6-a_1 & 1-a_2a_5 & a_1a_5-a_6 \\ a_1a_3-a_2 & a_2a_4-a_3 & 1-a_1a_4 \end{bmatrix} \begin{bmatrix} R-b_1 \\ G-b_2 \\ B-b_3 \end{bmatrix}, \quad (2)$$

3 *Determinant of the inverse matrix*

$$4 K = 1 + a_1a_3a_5 + a_2a_4a_6 - (a_1a_4 + a_2a_5 + a_3a_6). \quad (3)$$

5



6

7 **Fig. 2** Flow velocity vector distribution obtained by inter-color 3-D cross correlation for a wake  
8 behind a delta wing of 25 degree in angle of attack at which periodic stall occurred.

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## 10 **References**

- 11 Pick S, Lehmann F (2009) Stereoscopic PIV on multiple color-coded light sheets and its application to axial flow in  
12 flapping robotic insect wings. *Exp Fluids* 47: 1009-1023.
- 13 Watamura T, Tasaka Y, Murai Y (2013) LCD-projector based 3D color PTV. *Exp Thermal Fluid Sci* 47: 68-80.
- 14 Charonko J, Antoine E, Vlachos PP (2014) Multispectral processing for color particle image velocimetry. *Microfluid*  
15 *Nanofluid* 17: 729-743.
- 16 Aguirre-Palbo AA, Alarfaj, MK, Li EQ, Hernandez-Sanchez JF, Thoroddsen ST (2017) Tomographic particle image  
17 velocimetry using smartphones and colored shadows. *Sci Reports* 7: 3714-3722.
- 18 Xiong J, Aguirre-Pablo AA, Idoughi R, Thoroddsen ST, Heidrich W (2021) Rainbow PIV with improved depth  
19 resolution – design and comparative study with Tomo PIV. *Meas Sci Tech* 32: 025401.